

ERRATA for VARIANCE COMPONENTS (1st Printing)

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ABSTRACT

Corrections to a book.

**Page/Line**

vii/16: After restricted add (or residual) [There is room on the line.]

7/2: Penultimate word: fitted should be filled [ll not tt] .

17/Table 1.6, line 7 of body of table: delete space in  $\alpha_1 E(e_{ij})$  so as to have

$$E(e_{ij}|\alpha_1) = \alpha_1 E(e_{ij}) = 0$$

45/5: referred should be referred .

64/6, equation (68), before the equal sign:  $\text{var}(\hat{\sigma}_e^2)$  should be  $\text{var}(\hat{\sigma}_\alpha^2)$  [subscript  $\alpha$  not  $e$ ] .

64/7, equation(69), the last symbol:  $\sigma_e^2$  should be  $\sigma_e^4$  [superscript 4 not 2] .

64/11, equation (71), the last symbol:  $\sigma_e^2$  should be  $\sigma_e^4$  [superscript 4 not 2] .

64/13, equation (72), the last symbol:  $-2\hat{\sigma}_e^2$  should be  $-2\hat{\sigma}_e^4$  [superscript 4 not 2] .

65/4 up, the right-most expression:  $\frac{F}{F_U} - 1$  should be  $\frac{F}{F_L} - 1$  [on denominator F subscript L not U] .

74/15, equation (96), numerator:  $-2\sigma_e^2$  should be  $-2\sigma_e^4$  [superscript 4 not 2] .

75/3, equation (101), middle term:  $\sigma_e^2$  should be  $\sigma_e^4$  [superscript 4 not 2] .

75/8, equation (102), right-most terms:  $]\sigma_\alpha^4$  should be  $\sigma_\alpha^4]$  .

86/9 up:  $-[E(\hat{\sigma}_e^2)]^2$  should be  $-[E(\tilde{\sigma}_e^2)]^2$  [tilde not hat, i.e.,  $\sim$  not  $\hat{\cdot}$ ] .

87/12 up, equation (132c):  $\sum$  should be  $\sum_i$  [subscript i] — TWICE.

in second term, denominator  $\lambda_i^2$  should be  $2\lambda_i^2$  [add 2] .

89/Table 3.10:

3rd line, 1st term:  $\mu, \sigma_e^2$  should be  $\mu, \sigma_\alpha^2$  [on the subscript  $\sigma^2$ , subscript  $\alpha$  not e] .

4th line, 3rd term after = sign:  $\bar{y}$  . should be  $\bar{y}_i$  . [on  $\bar{y}$  superscript i . not .] .

5th line, 2nd term after = sign:  $n_i(\bar{y}_i - \mu)^2$  should be  $n_i^2(\bar{y}_i - \mu)^2$  [ $n_i^2$  not  $n_i$ ] .

92/15: Move the (146) up to be level with the line of space that is between the two “displayed” lines.

In the first of those “displayed” lines the  $>$  should be  $\geq$  .

In the second of those “displayed” lines the  $\leq$  should be  $<$  .

94/12 up, the equation which follows the partial line of text that comes after equation (150):

underneath (150): add (151) so as to have

$$\tilde{\sigma} = (1 - 1/n)s^2 \quad (151)$$

110/1: Derive  $L(\mu, \sigma^2|s^2)$  should be Derive  $L(\sigma^2|s^2)$  [delete  $\mu$ ] .

110/18, 2nd line of (a) of E3.24: estimators should be estimates .

110/E3.25, line 2, last symbol: 0 should be bold [bold zero] .

line 3, after a,: add: and with every  $\mathbf{e}_i$  and  $\mathbf{e}_j$ , having zero covariance,

lines 4, 5, and 6: align (i), (ii) and (iii) to the right

align the corresponding  $\text{var}(\mathbf{e}_i)$  to the left so as to have

$$(i) \quad \text{var}(\mathbf{e}_i) =$$

$$(ii) \quad \text{var}(\mathbf{e}_i) =$$

$$(iii) \quad \text{var}(\mathbf{e}_i) =$$

115/last, last expression:  $wabc$  (Rule 8) should be  $wabc$  (Rule 8)  $- 1$  [add  $- 1$ ] .

117/4 up:  $MS(A:B)$  should be  $MS(AB)$  [delete :] .

154/7, after the first = sign:  $\mathbf{1}'_s$  should be  $\mathbf{1}_s$  [delete prime] .

163/19, equation (107):  $\mathbf{X}(\mathbf{X}'\mathbf{X}) - \mathbf{X}'\mathbf{y}$  should be  $\mathbf{X}(\mathbf{X}'\mathbf{X})^{-1} - \mathbf{X}'\mathbf{y}$

[Must be identical to (107) on page 159.]

163/20, equation (110):  $\mathbf{X}(\mathbf{X}'\mathbf{V} - \mathbf{X})^{-1} - \mathbf{X}'\mathbf{V}^{-1}\mathbf{y}$  should be  $\mathbf{X}(\mathbf{X}'\mathbf{V}^{-1}\mathbf{X})^{-1} - \mathbf{X}'\mathbf{V}^{-1}\mathbf{y}$

[Must be identical to (110) on page 160.]

164/9, part (c) of E4.4:  $\beta_j'^2$  should be  $\dot{\beta}_j^2$  [dot above  $\beta$ , not superscript prime] .

166/exercise E4.18:

Delete all 3 lines of part (c).

Relabel part (d) as part (c).

After item (ii) of part (d) [which is now (c)] add:

(iii) Write down the terms of  $\mathbf{V} = \text{var}(\mathbf{y})$  that involve the variance components  $\sigma_{\mathbf{M}:\text{CB}}^2$ ,  $\sigma_{\mathbf{F}:\text{C}}^2$  and  $\sigma_{\mathbf{FM}:\text{CB}}^2$ . Use Kronecker products of  $\mathbf{I}$ -matrices and  $\mathbf{J}$ -matrices.

171/equation (4): Delete the penultimate  $+$  sign and close up so as to have  $\left\}_{j=1}^b \left\}_{i=1}^a \gamma + \mathbf{e}$  .

178/equation (23), after the  $=$  sign, first row, second term:

$-2\sigma_e^2$  should be  $-2\sigma_e^4$  [superscript 4 not 2] .

219/equation (144), the 1st denominator:  $a$  should be  $b$  .

the 2nd denominator:  $b$  should be  $a$  .

251/last, just prior to the 3rd  $=$  sign:  $\mathbf{Z}_j \mathbf{Z}_j \sigma_j^2$  should be  $\mathbf{Z}_j \mathbf{Z}_j' \sigma_j^2$  [add a prime] .

259/8, 3rd word: normally should be normal [delete ly] .

261/4, last term:  $\mathbf{DZ}'$  should be  $\mathbf{ZD}$  .

262/10: Change this line to be:  $= E_{\mathbf{y}}\{(\tilde{\mathbf{u}} - \mathbf{u}_0)' \mathbf{A}(\mathbf{u}_0 - \mathbf{u}_0)\} = \mathbf{0}$  [Delete  $E_{\mathbf{u}}$ , delete square brackets, use round parentheses, add a prime, zero is to be bold.]

262/11: Change this line to be: since, given  $\mathbf{y}$ , only  $\mathbf{u}|\mathbf{y}$  is not fixed with  $E_{\mathbf{u}}(\mathbf{u}|\mathbf{y}) = \mathbf{u}_0$ . Therefore

*Note to editor:* If this is too much for the one available line then cut the “with  $E_{\mathbf{u}}(\mathbf{u}|\mathbf{y}) = \mathbf{u}_0$ ”.

290/6 of Section 8.1: (28) should be (27a) .

(103) should be (89) .

(104) should be (90) .

303/7 up:  $\mathbf{B}^{-1} \rightarrow \mathbf{0}$  should be  $\mathbf{B}^{-1} \rightarrow \mathbf{0}$  [bold zero] .

308/7, equation (42), 1st term:  $\mathbf{u}_1' \mathbf{u}_1$  should be  $\mathbf{u}_1' \mathbf{u}_1$  [subscript i not 1] .

314/exercise E8.7, second line:  $\text{tr}(\mathbf{Z}_i \mathbf{P} \mathbf{Z}_i') \leq \text{tr}(\mathbf{Z}_i \mathbf{V} \mathbf{Z}_i')$  should be  $\text{tr}(\mathbf{Z}_i' \mathbf{P} \mathbf{Z}_i) \leq \text{tr}(\mathbf{Z}_i' \mathbf{V}^{-1} \mathbf{Z}_i)$

[On each side of the  $\leq$  sign, prime should be on 1st  $\mathbf{Z}_i$  not the last.]

367/9 of 2nd paragraph:  $P_i$  should be  $p_i$  [lower case, italic] .

372/equation under (10): subscript to f should be y|p not p|y .

378/3 up, after the 1st = sign:  $\sigma_\alpha^2 \mathbf{I}_a$  should be  $\sigma_{\alpha_1}^2 \mathbf{I}_a$

[On  $\sigma^2$ , the subscript  $\alpha$  needs a subscript 1 (one), akin to the subscript 2 in the last line.]

384/2, first term:  $2\mathbf{l}_\beta$  should be  $2\mathbf{l}_\beta$  [el should not be bold – see (24)] .

390/Table 11.1, footnote: Hooking should be Hocking [oc not oo] .

395/4 up, equation (52):  $\{\mathbf{d}$  should be  $\{\mathbf{r}$  [r not d] .

397/equation (59), immediately after = sign:  $\{\mathbf{d}$  should be  $\{\mathbf{c}$  [c not d] .

398/equation (60), immediately after = sign:  $\{\mathbf{d}$  should be  $\{\mathbf{c}$  [c not d] .

407/equation (8):  $\sigma^2$  should not be bold .

407/two lines above equation (10): the middle E should be feint italic not bold Roman.

410/4 up, equation (22):  $\mathbf{T}_A$  should be  $\mathbf{T}_4$  [4 not A]

421/5 up: In Brown (1976), 1978) should be Brown (1976, 1978) [No parens before the comma.]

445/8 up: Move the  $a_k$  to the right to be under the zeros.

448/4 below equation (6): (ii) should be (iii) .

449/2 below equation (17): threom should be theorem .

453/Equation (29), right-hand side of the = sign: the + should be –  
the – should be +

Thus the equation will be

$$(\mathbf{D} + \lambda \mathbf{t} \mathbf{t}')^{-1} = \mathbf{D}^{-1} - \frac{\mathbf{D}^{-1} \mathbf{t} \mathbf{t}' \mathbf{D}^{-1}}{1/\lambda + \mathbf{t}' \mathbf{D}^{-1} \mathbf{t}}$$

453/3, equation (27), immediately after + sign:

$$\begin{bmatrix} -\mathbf{A}^{-1} \\ \mathbf{0} \end{bmatrix} \text{ should be } \begin{bmatrix} -\mathbf{A}^{-1} \mathbf{B} \\ \mathbf{I} \end{bmatrix} \quad \begin{array}{l} [\text{add } \mathbf{B}] \\ [\mathbf{I} \text{ not } \mathbf{0}] \end{array} .$$

480/6 up, last name VonKrosig should be von Krosigk [lower case v, space after von, add final k] .